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# Verification of Systems With Non-Boolean Variables

## *How to find errors in computer programs*

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# Introduction

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- ◆ More and more products contain **embedded computers**:
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- ◆ Designed by humans  $\implies$  May contain errors
- ◆ Types of errors:
  - Irritating/harmless
  - Catastrophic



# Catastrophic Errors

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## **Therac-25 radiation therapy machine [1985–1987]**

- ◆ Patients receive massive overdoses of X-rays
- ◆ Two deaths, others injured and handicapped



# Catastrophic Errors

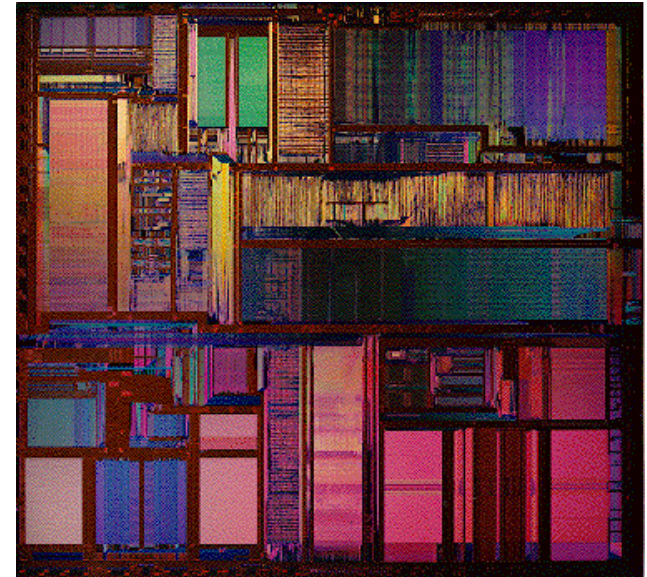
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## Intel's Pentium division bug [Dec. 1994]

- ◆  $4.9999999/14.9999999$  gives 0.333329, but should be 0.33333329
- ◆ Intel have to replace millions of defect processors
- ◆ Costs several 100 million \$



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- ◆ Costs ESA 600 million \$





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## **NASA's Mars Climate Orbiter [23 Sep. 1999]**

- ◆ One team uses English units, another metric units
- ◆ Landing procedure doesn't start timely
- ◆ Spacecraft explodes in Mars's atmosphere



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- ◆ 10 years ago: Testing and simulation
- ◆ But testing only shows the presence of errors, not the absence of errors



# Formal Verification

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  - Construct a mathematical *model* of the system
  - Specify the *requirements*
  - *Prove* that the model satisfies the requirements



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- ◆ Proofs can be automated for programs with true/false variables
- ◆ Easy to check that “the processor divides correctly”





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- ◆ Perspective: Verification can be used to check Java programs



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## It's commercial

- ◆ Collaborate with researchers from SRI International
- ◆ Co-founder of the spin-off company  
[[www.configit-software.com](http://www.configit-software.com)] [1999]

